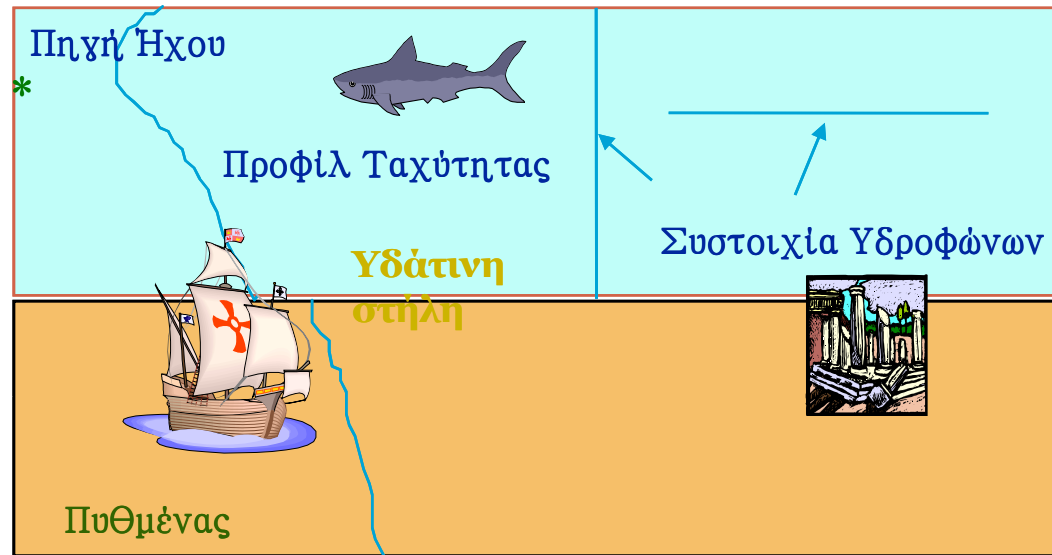


Εισαγωγή

Εισαγωγή στην Ακουστική Ωκεανογραφία



Εισαγωγή στην Ακουστική Ωκεανογραφία

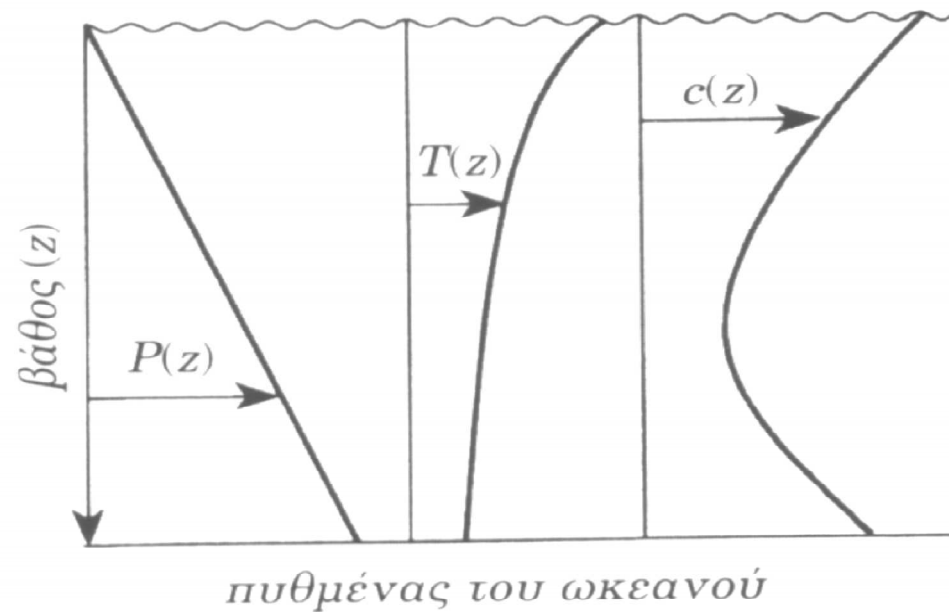
Ταχύτητα διάδοσης του ήχου στο νερό

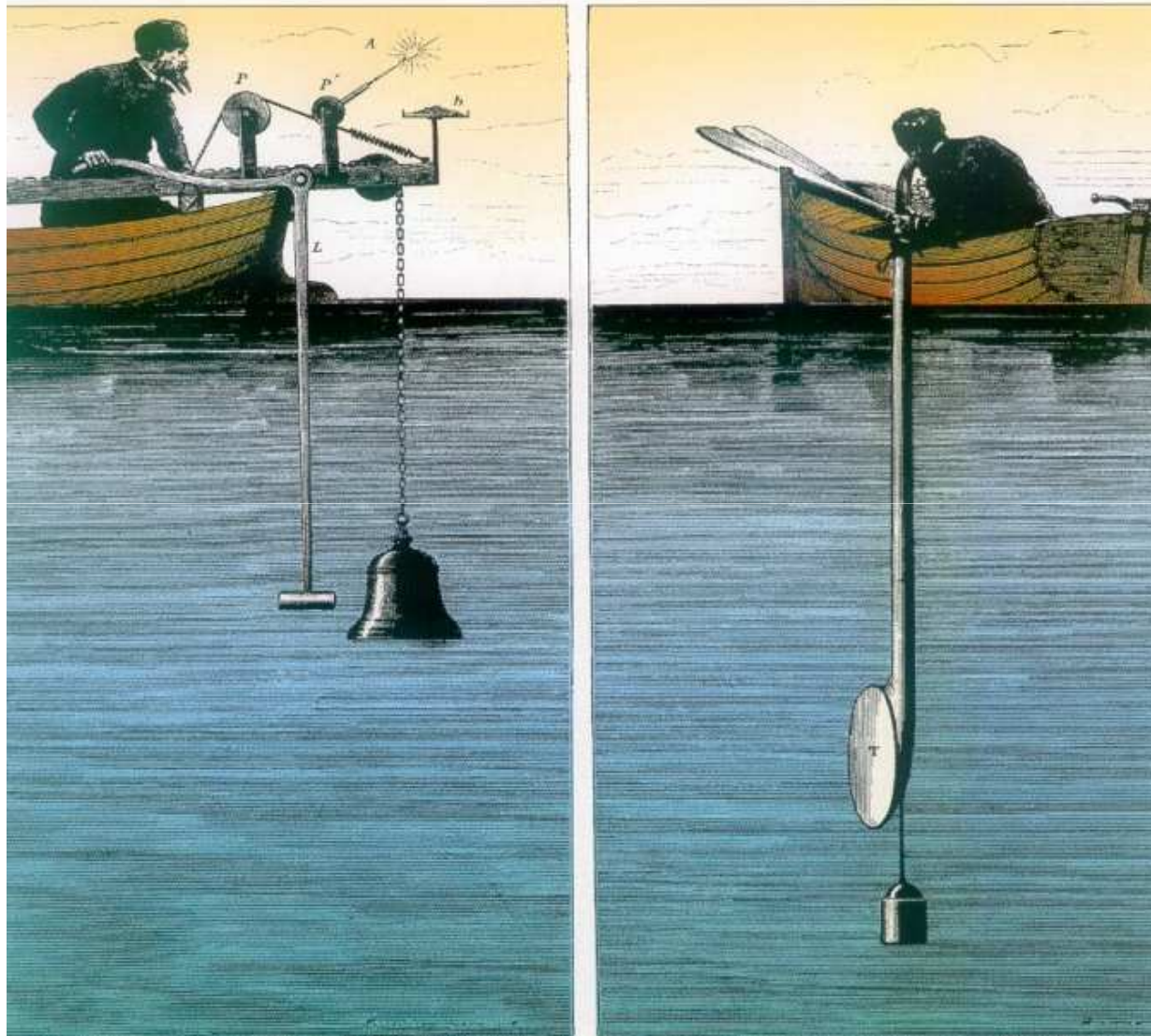
$$c = 1449.2 + 4.6 T - 0.055 T^2 + 0.00029 T^3 + (1.34 - 0.010T)(S - 35) + 0.016 z$$

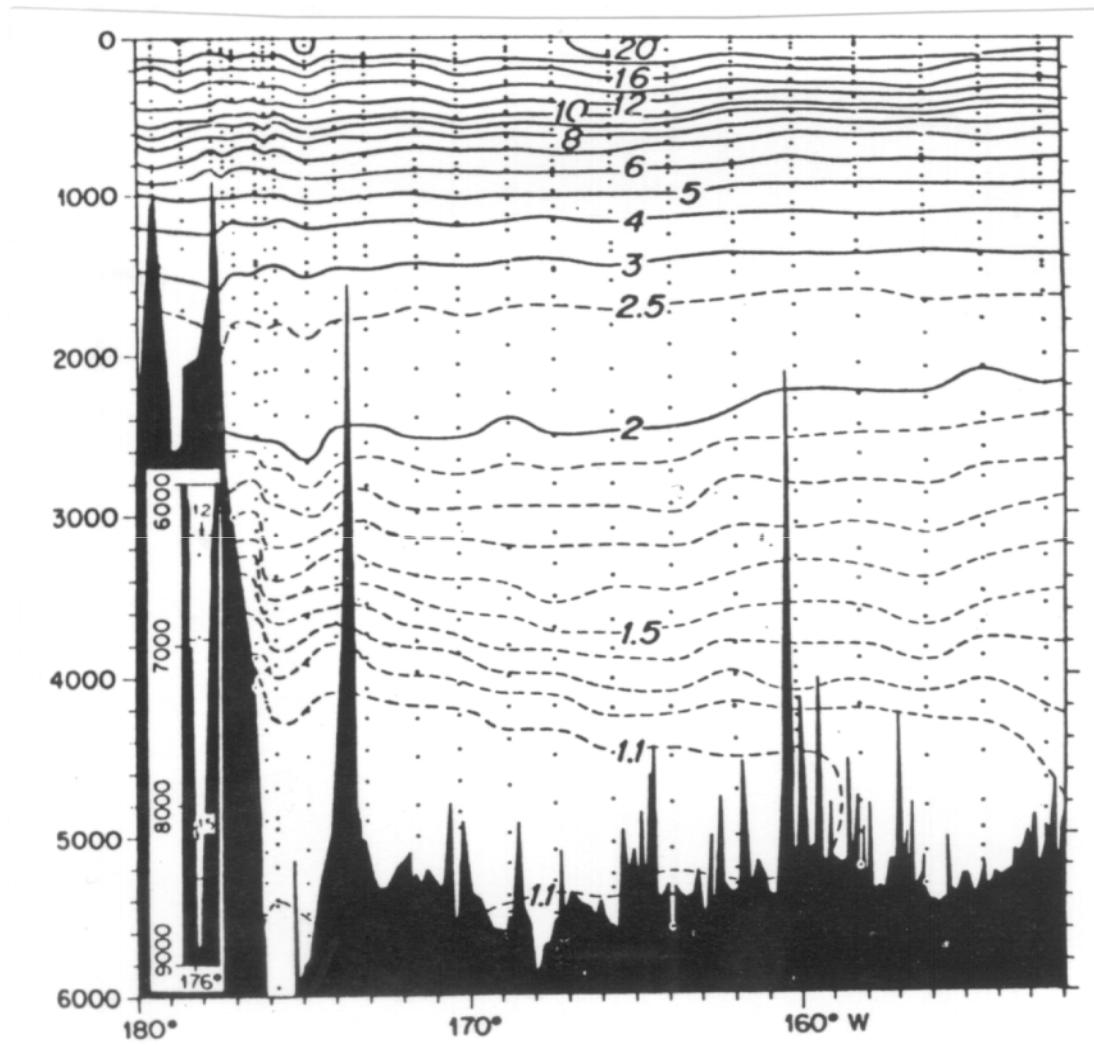
όπου c = ταχύτητα του ήχου (m/s)
 T = θερμοκρασία (°C)
 S = αλατότητα (σε μέρη επί τοις χιλίοις)
 z = βάθος (m)

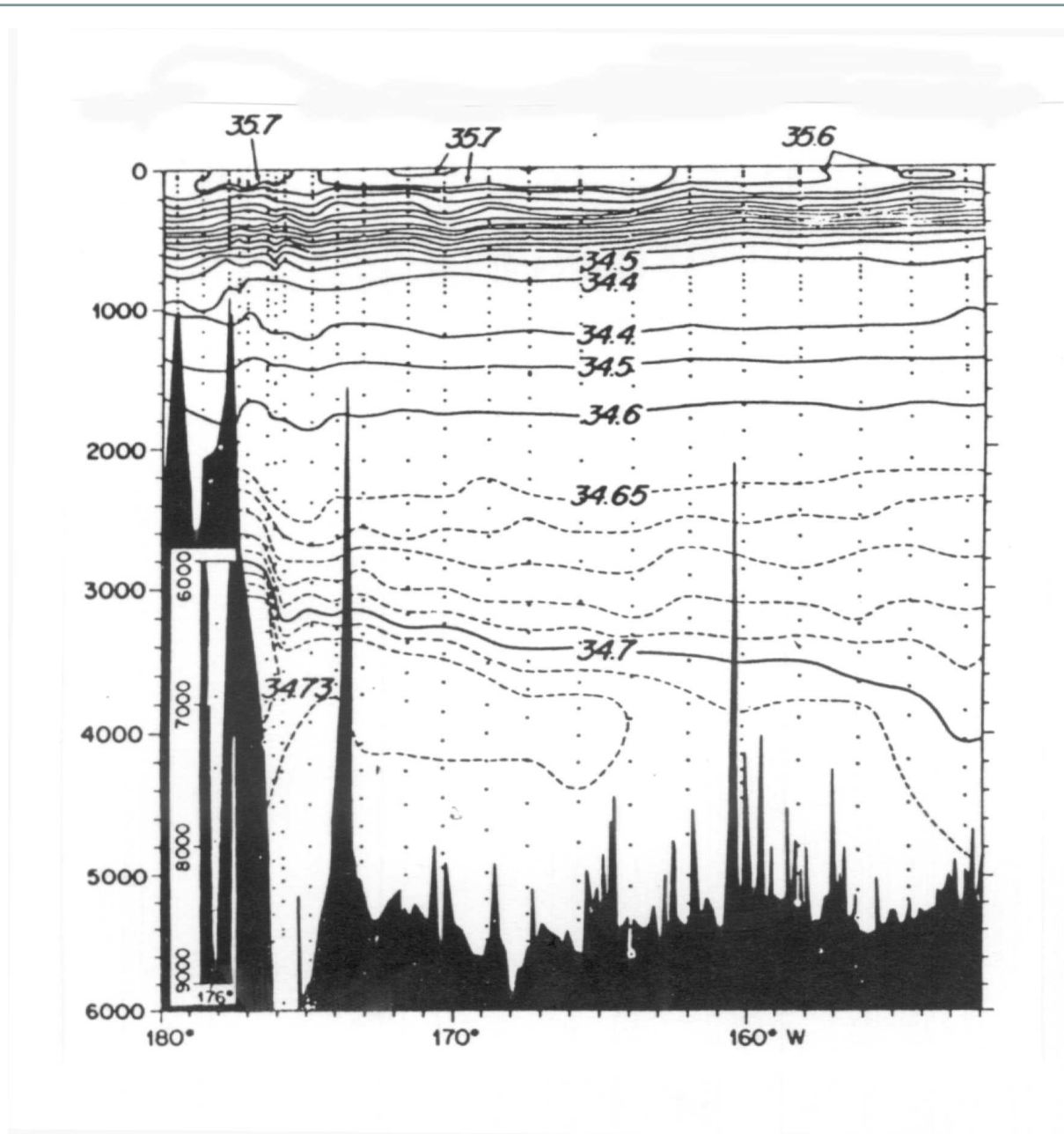
Η θερμοκρασία της θάλασσας και η πίεση
μεταβάλλονται με το βάθος

Η ταχύτητα διάδοσης εξαρτάται από τα μεγέθη
αυτά και συνεπώς μεταβάλλεται με το βάθος

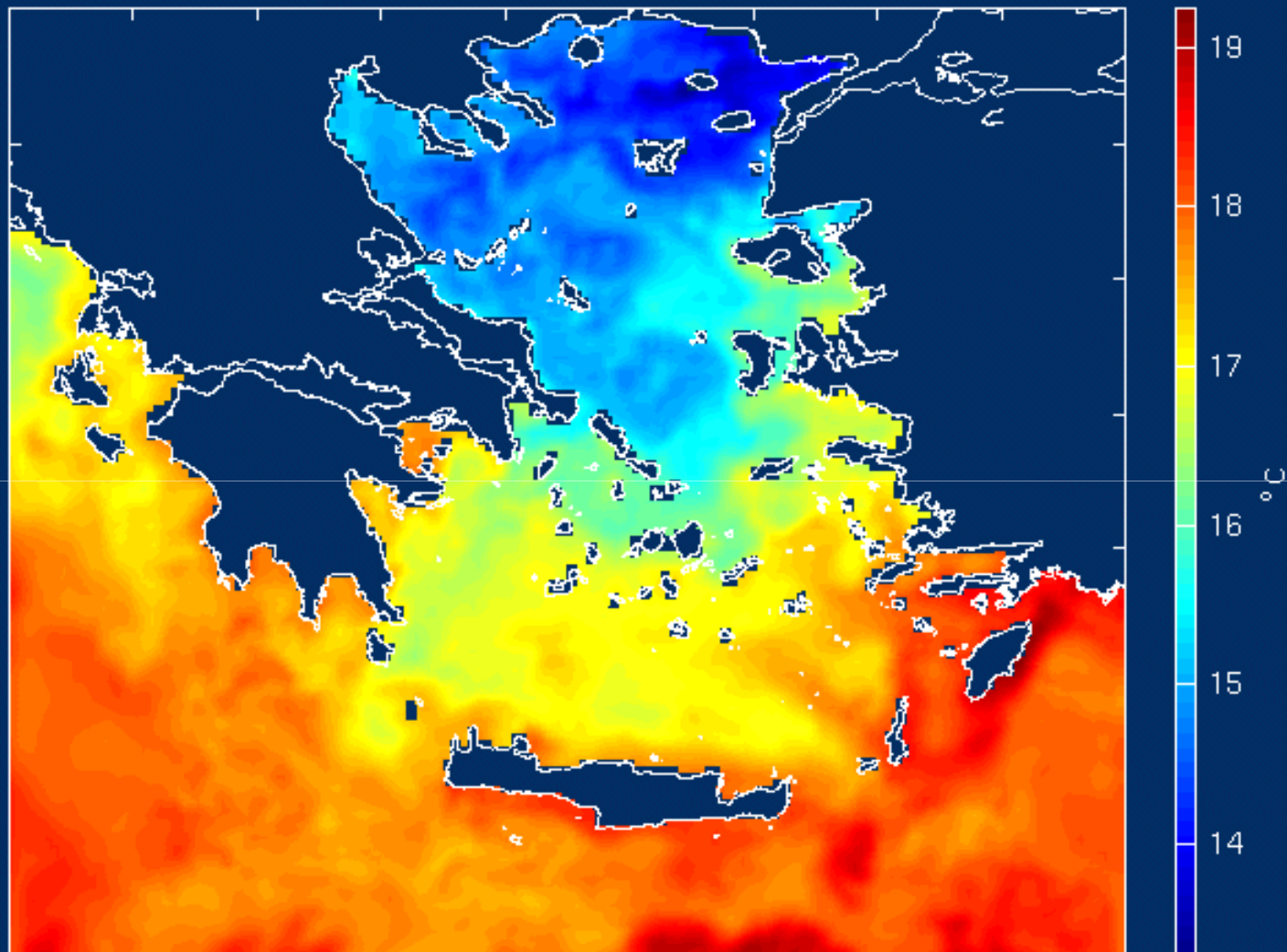






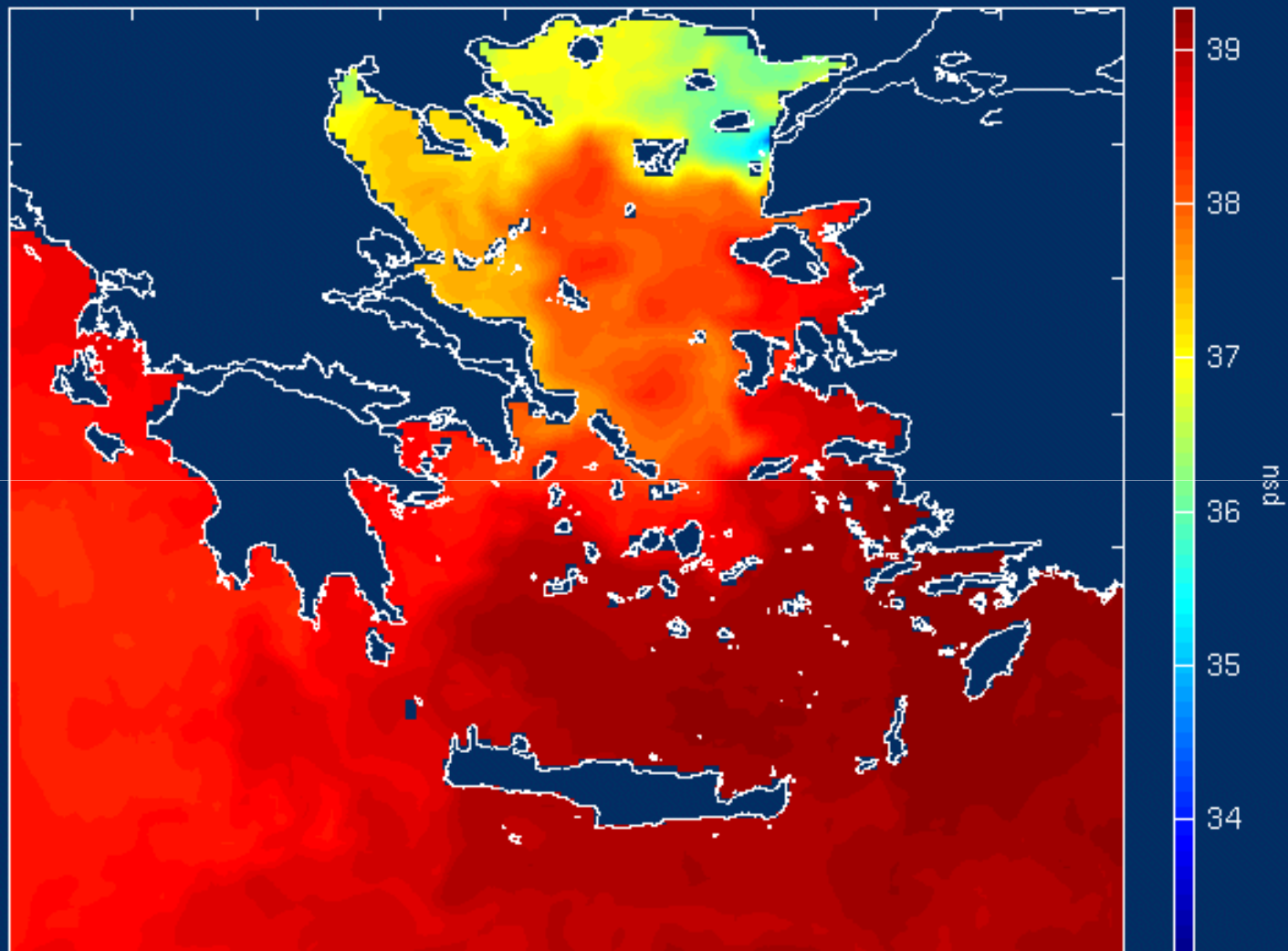


Επιφανειακή θερμοκρασία θάλασσας στις 14/12/05 Ώρα:18:00UTC



Ελληνικό Κέντρο Θαλασσιών Ερευνών, 19013, Ανάβυσσος
Σύστημα ΠΟΣΕΙΔΩΝ - <http://www.poseidon.hcmr.gr>

Επιφανειακή αλατότητα στις 15/12/05 Ώρα:12:00 UTC

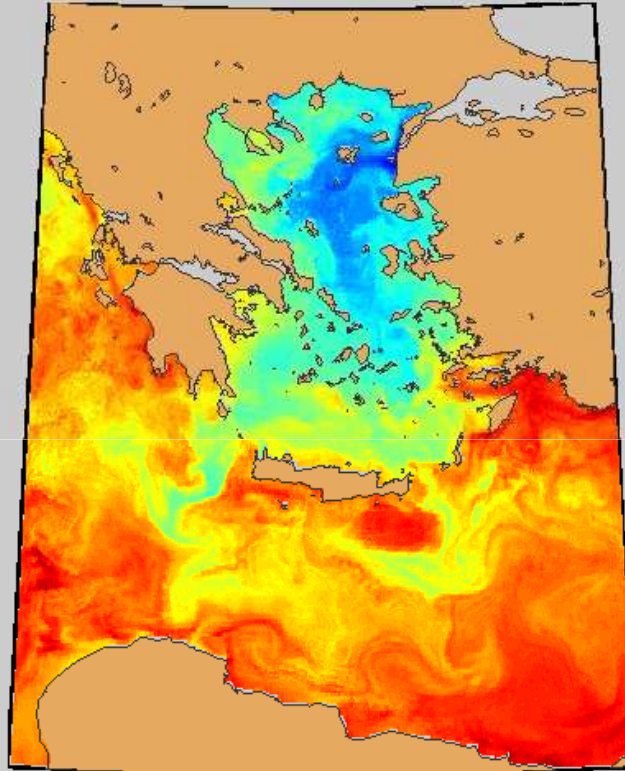


Ελληνικό Κέντρο Θαλασσιών Ερευνών, 19013, Ανάβυσσος
Σύστημα ΠΟΣΕΙΔΩΝ - <http://www.poseidon.hcmr.gr>

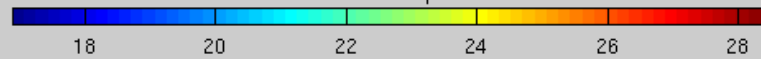


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Sunday (27/09/09) 00:00UTC



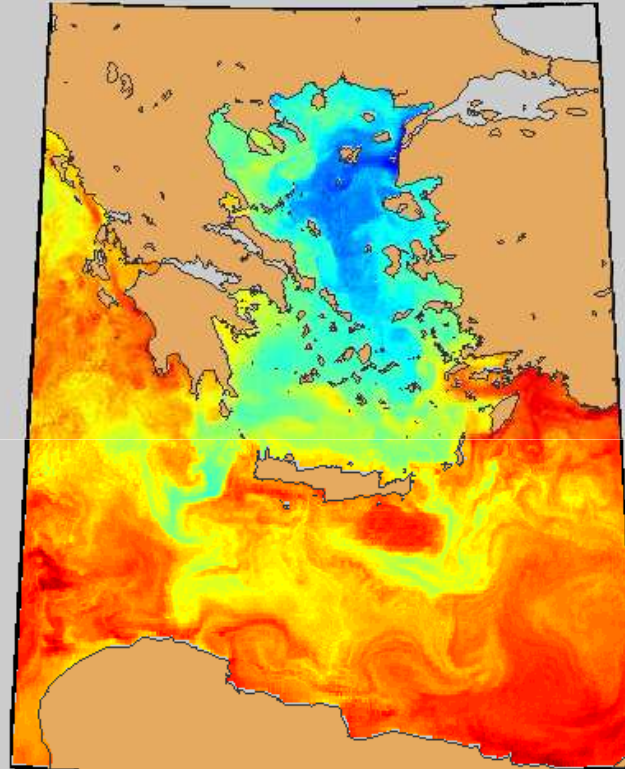
Color denotes Temperature in °C



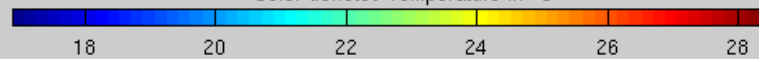


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Sunday (27/09/09) 06:00UTC



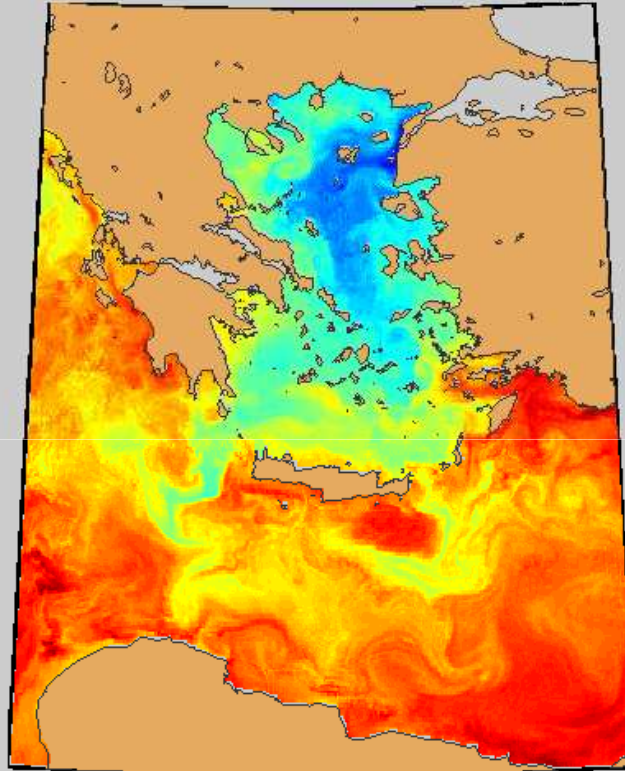
Color denotes Temperature in °C



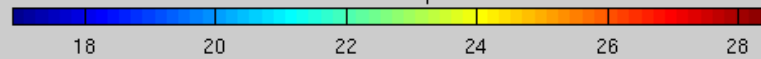


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Sunday (27/09/09) 12:00UTC



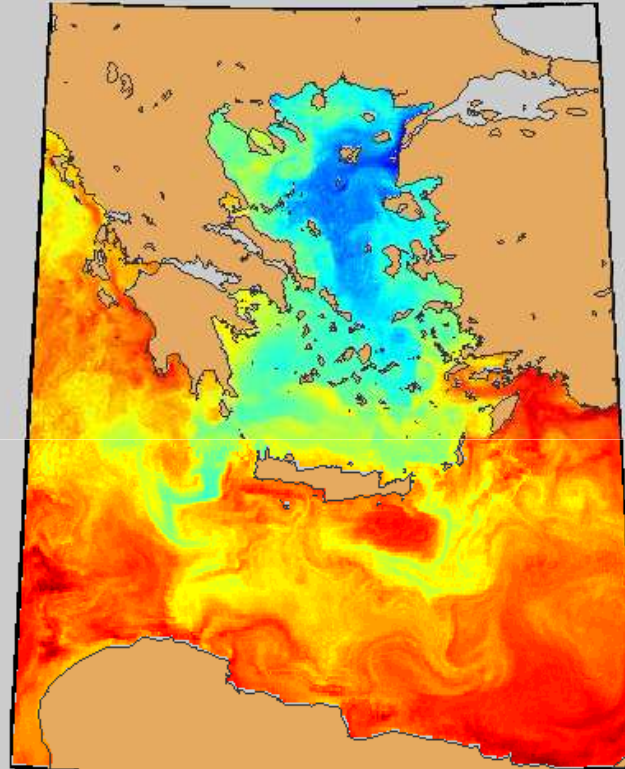
Color denotes Temperature in °C



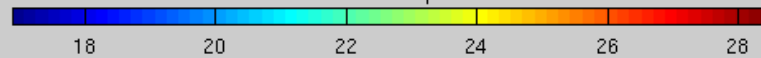


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Sunday (27/09/09) 18:00UTC



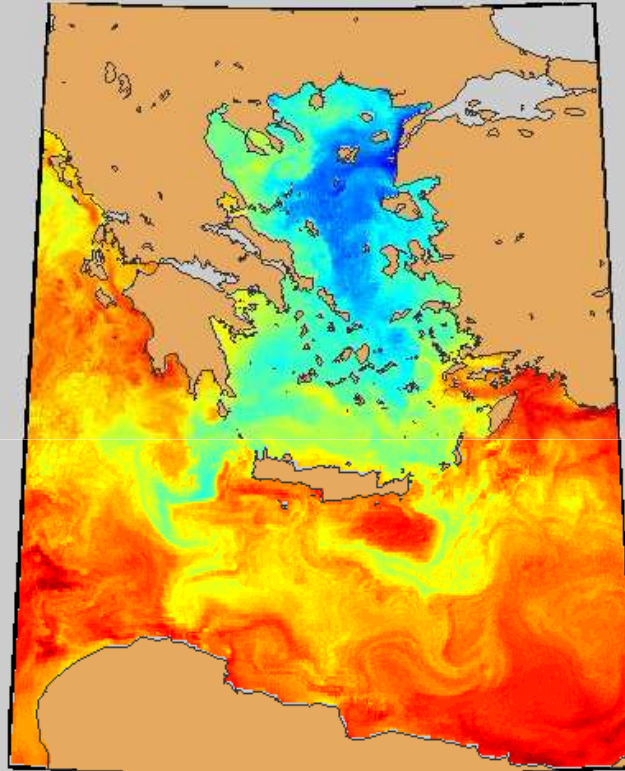
Color denotes Temperature in °C



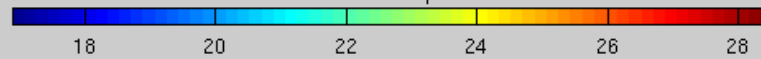


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Monday (28/09/09) 00:00UTC



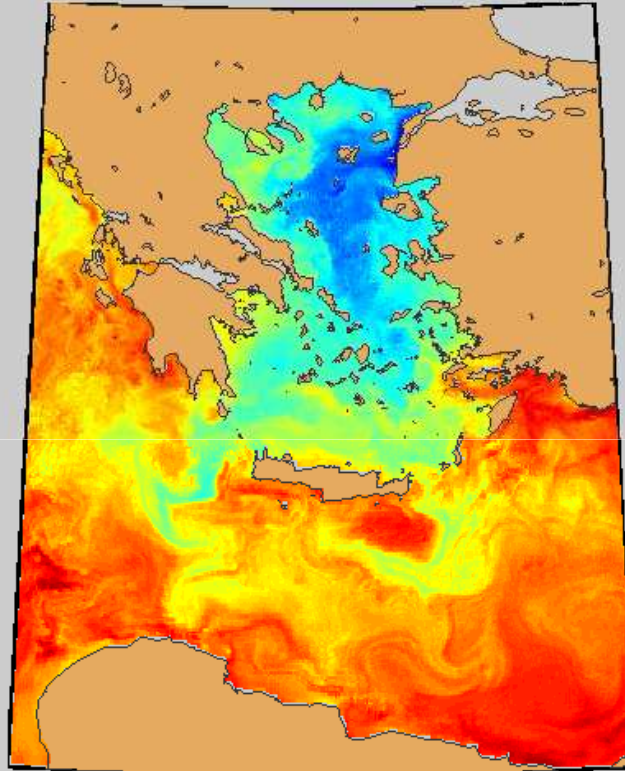
Color denotes Temperature in °C



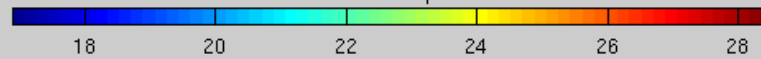


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Monday (28/09/09) 00:00UTC



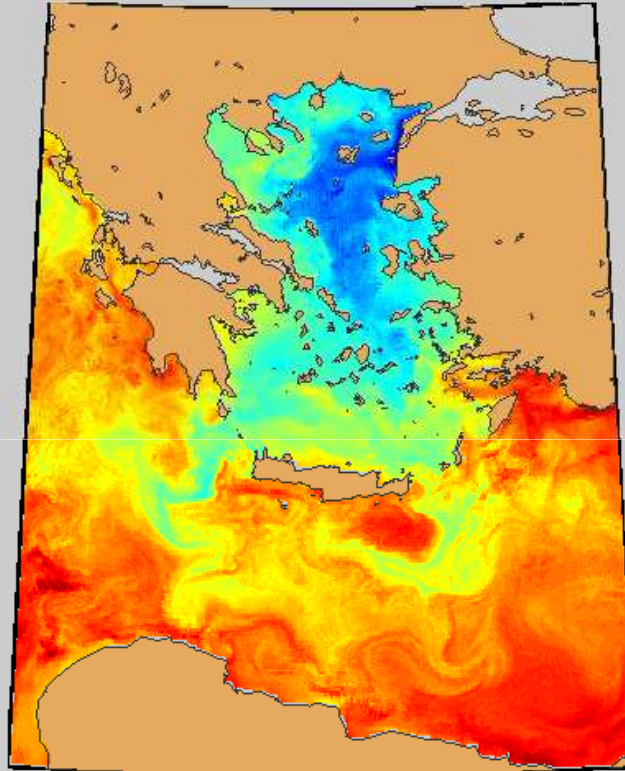
Color denotes Temperature in °C



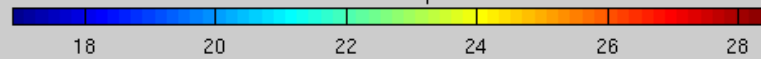


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Monday (28/09/09) 06:00UTC



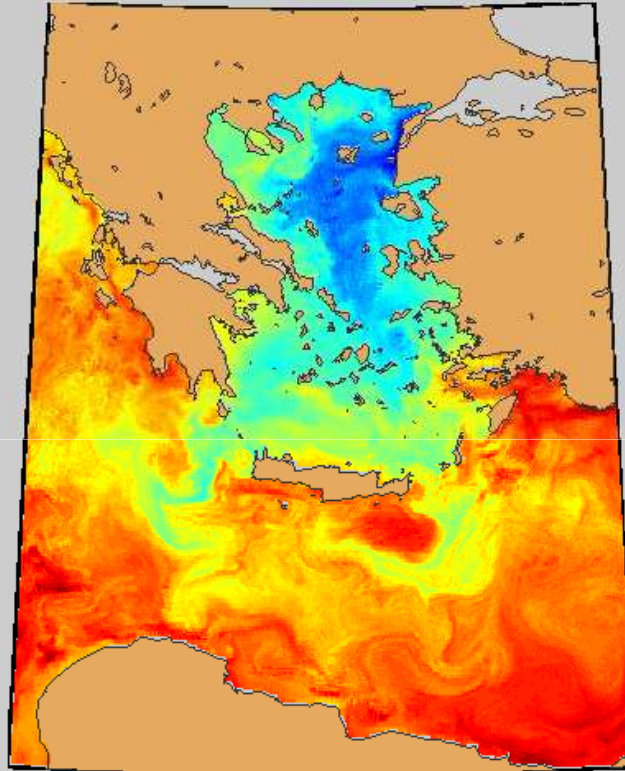
Color denotes Temperature in °C



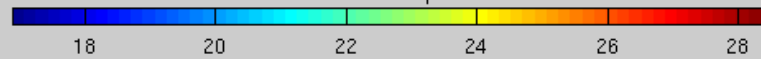


Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

Sea Surface temperature on Monday (28/09/09) 12:00UTC



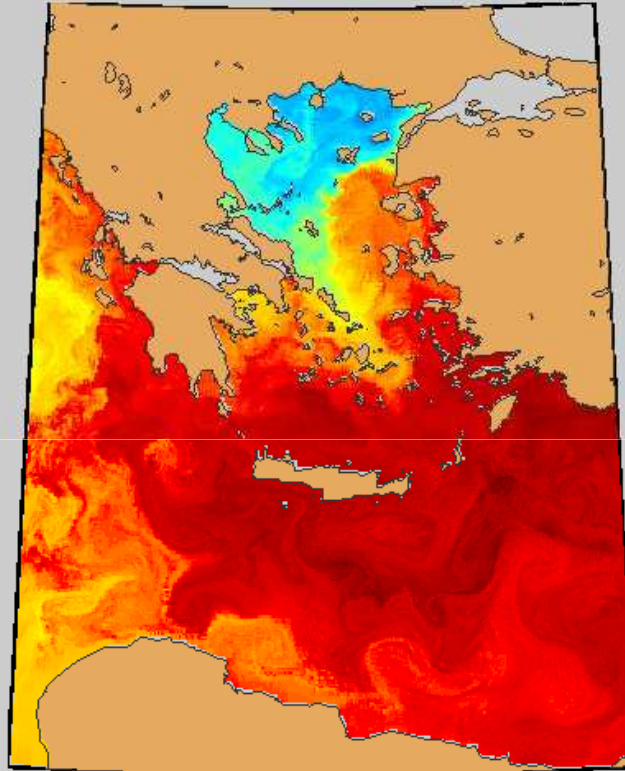
Color denotes Temperature in °C





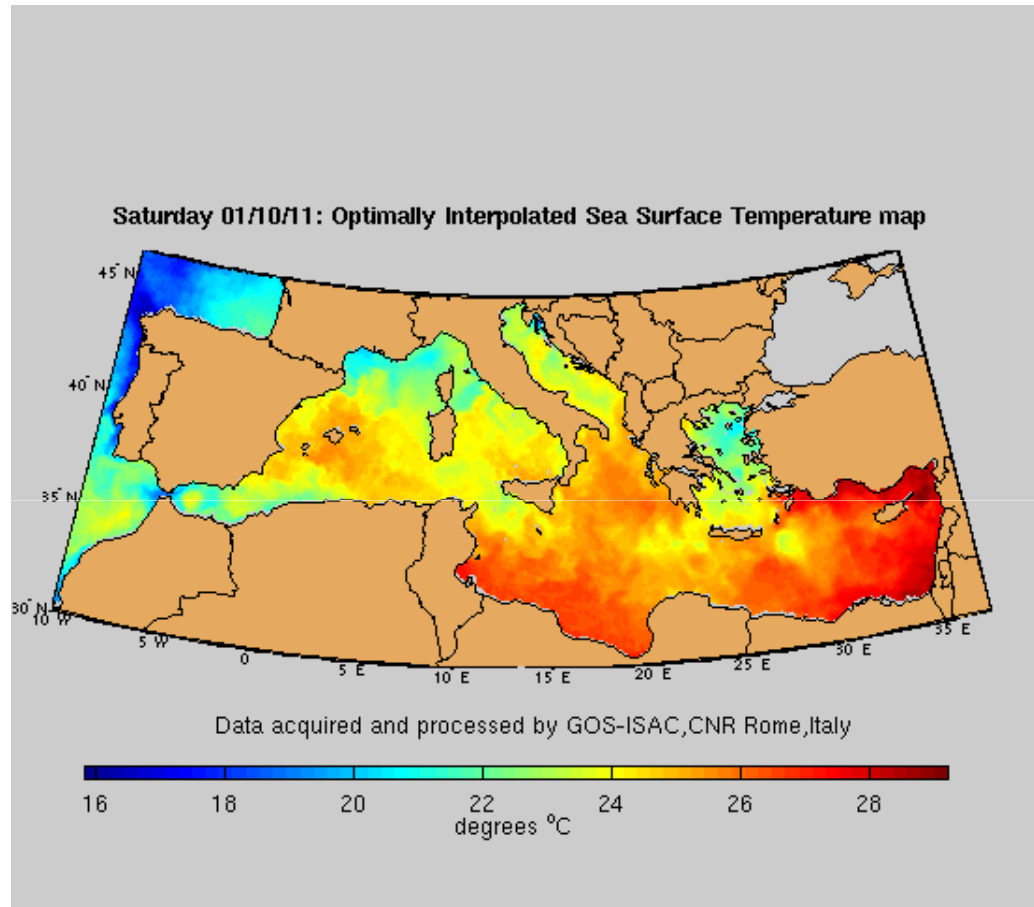
Hellenic Center for Marine Research, GR-19013, Anavissos, GREECE
POSEIDON System - <http://www.poseidon.hcmr.gr>

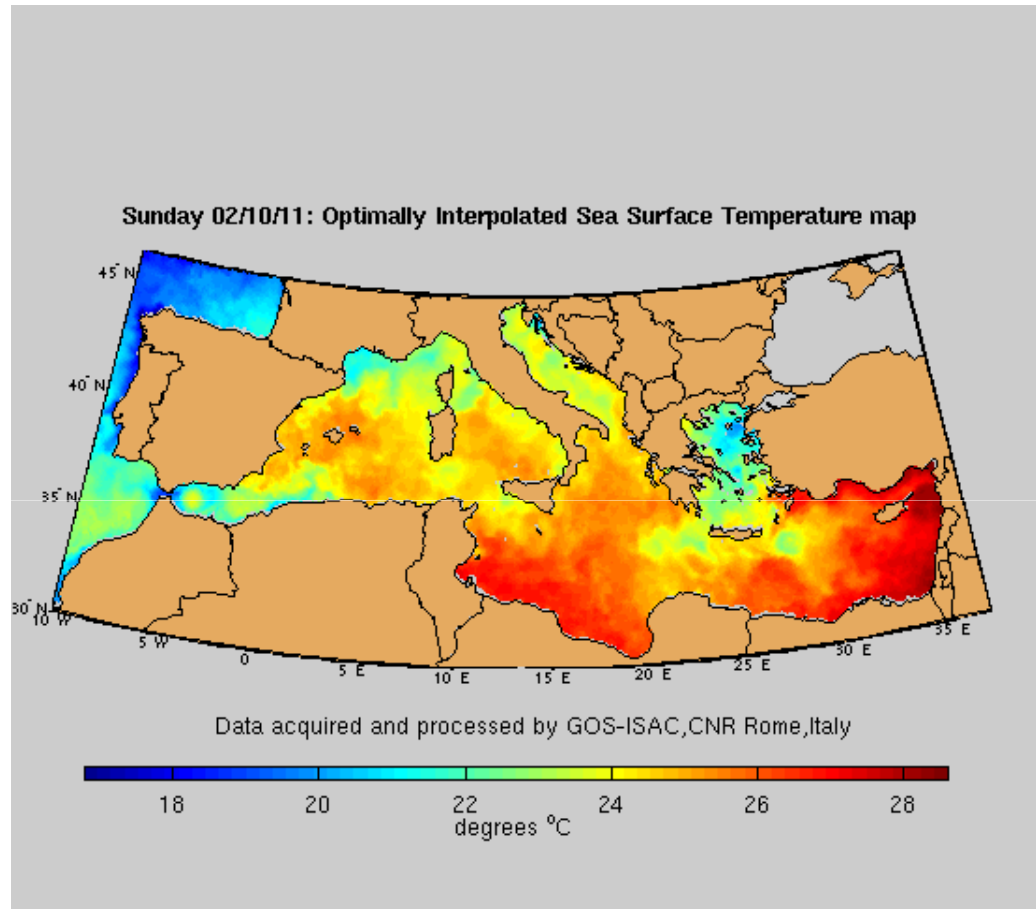
Sea Surface Salinity on Monday (28/09/09) 12:00UTC

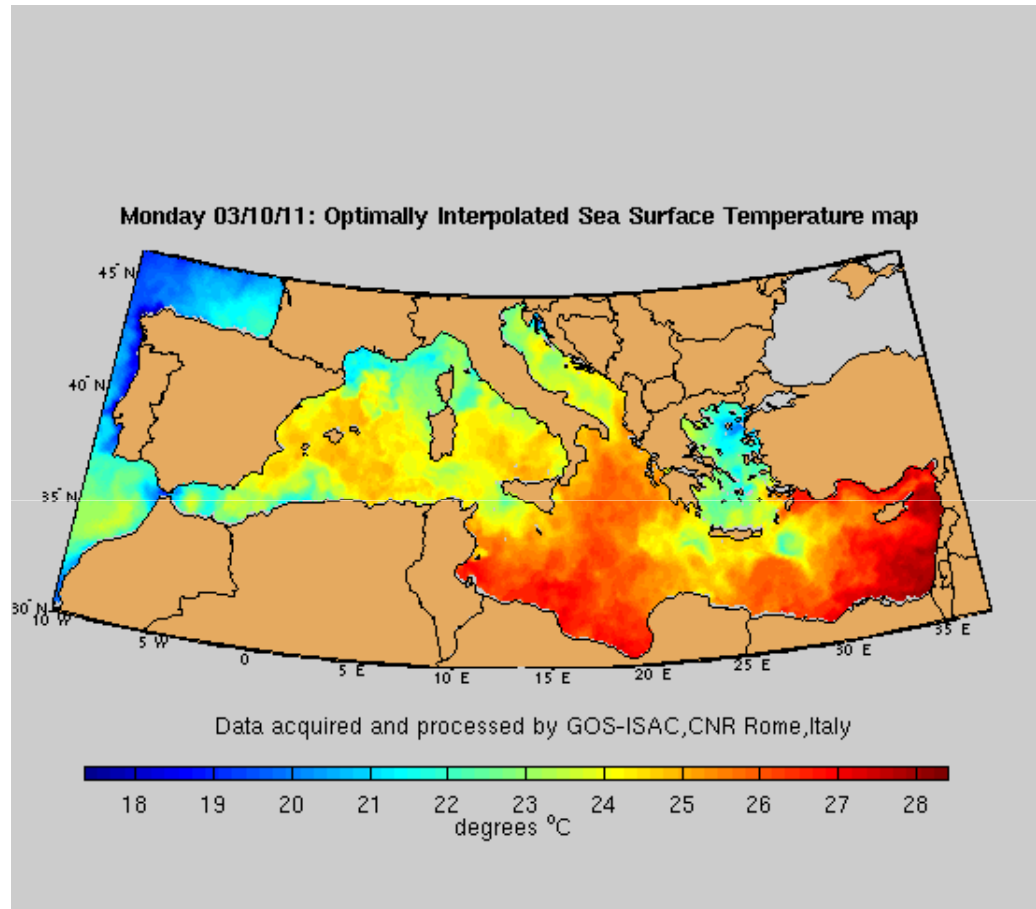


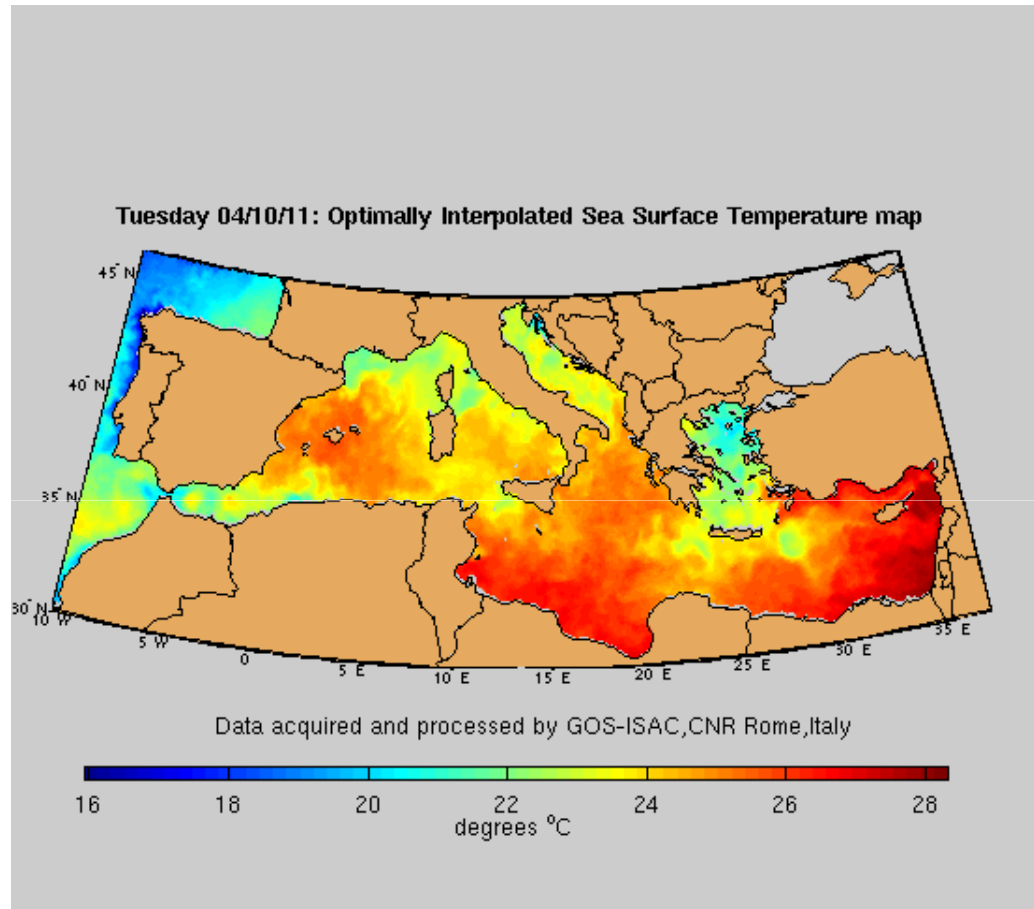
Color denotes Salinity in psu

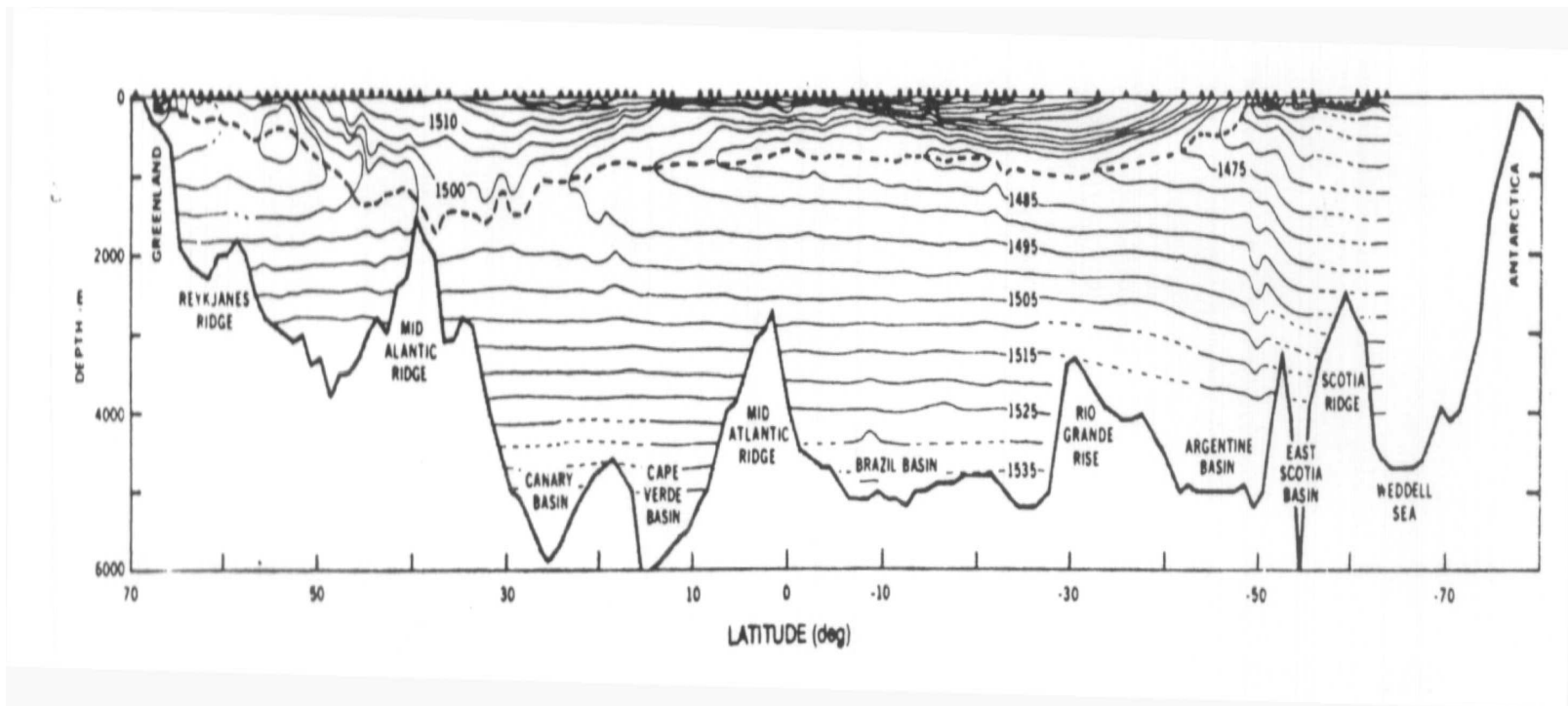


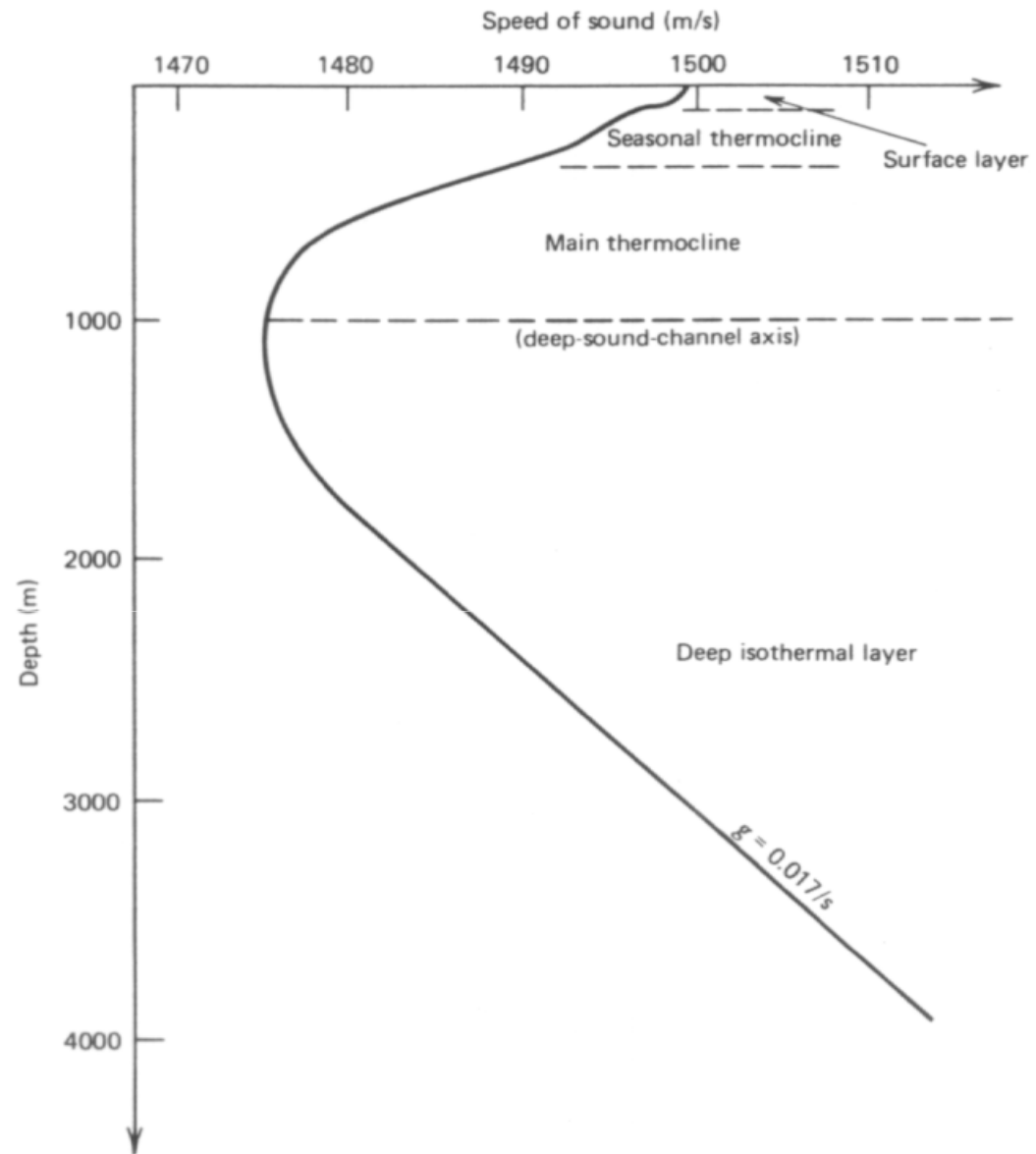


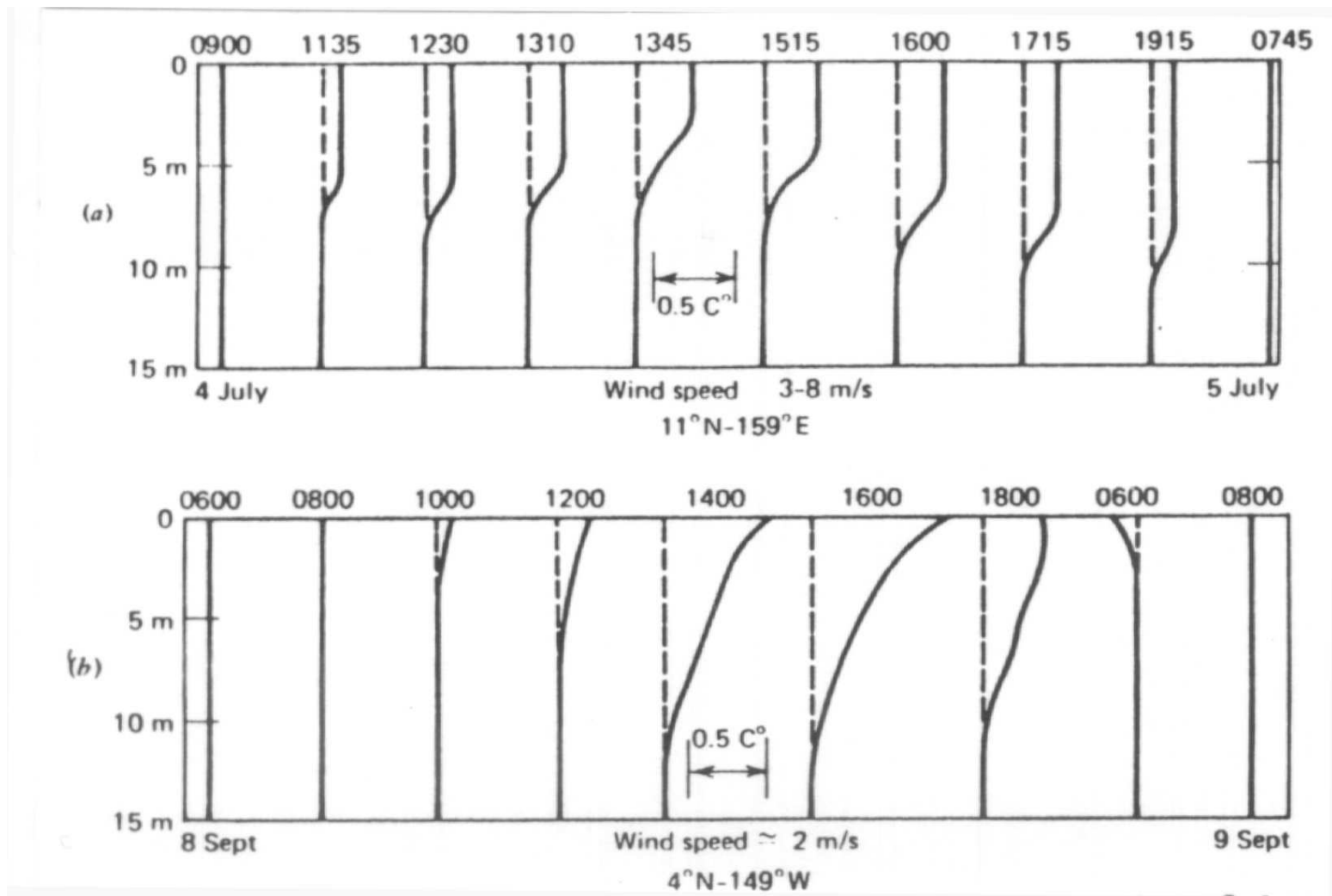












Κύματα Επιφανείας (Βαρύτητας και Επιφανειακής τάσης)



$$c = \sqrt{\frac{g}{k}}$$

όπου g είναι η επιτάχυνση της βαρύτητας = 9.8 m/s^2 και
 k είναι ο «αριθμός κύματος» οριζόμενος ως

$$k = \omega / c$$

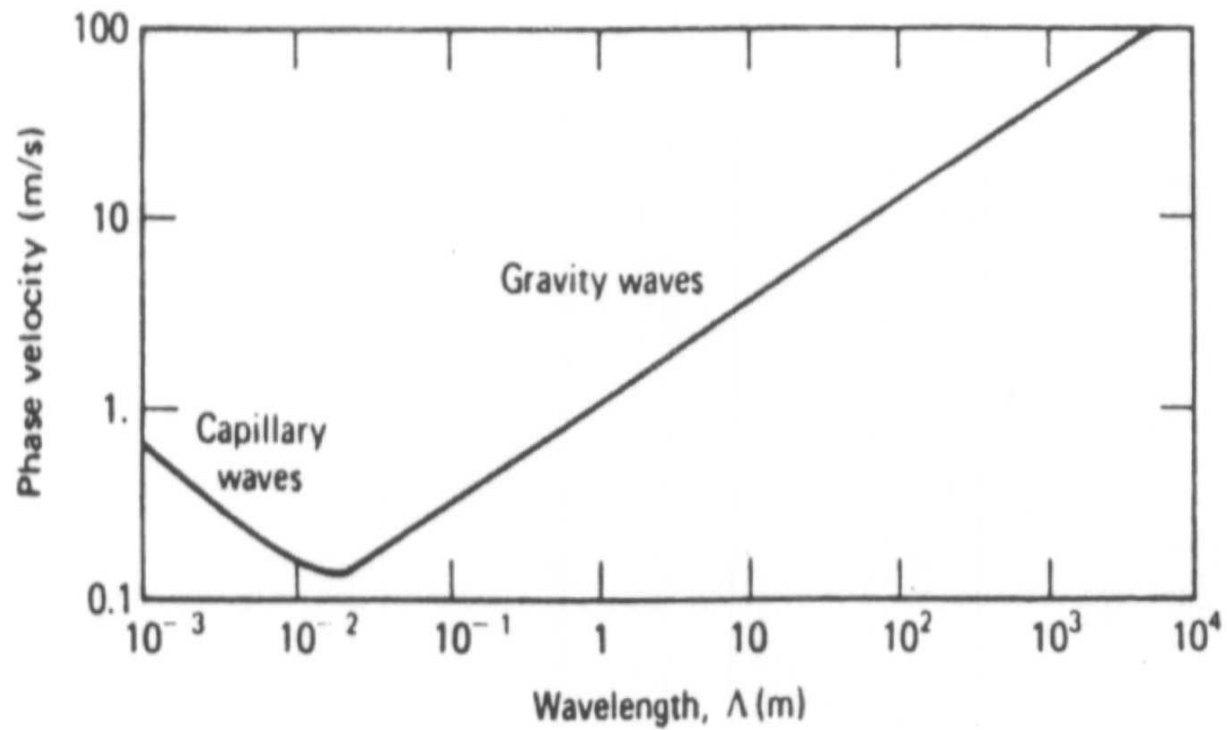
όπου ω είναι η κυκλική συχνότητα ($\omega = 2\pi f$)
 f είναι η συχνότητα σε Hz

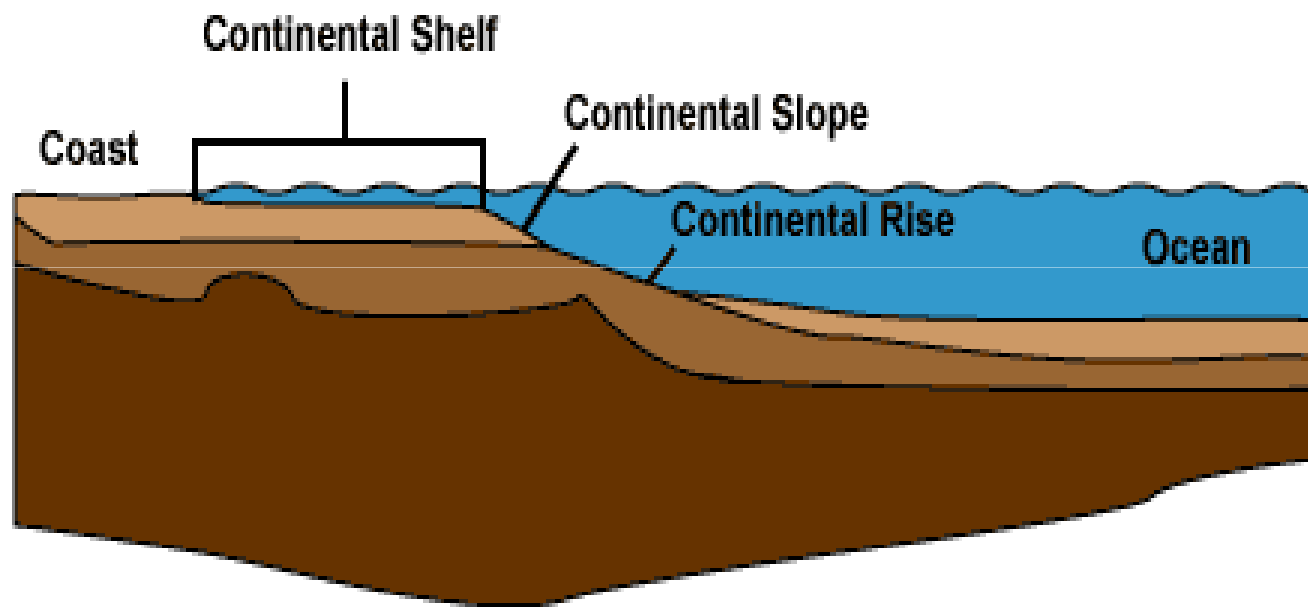
Στην περίπτωση που θεωρηθεί και η επιφανειακή τάση στον κυματισμό
τότε η φασική ταχύτητα δίδεται από την σχέση

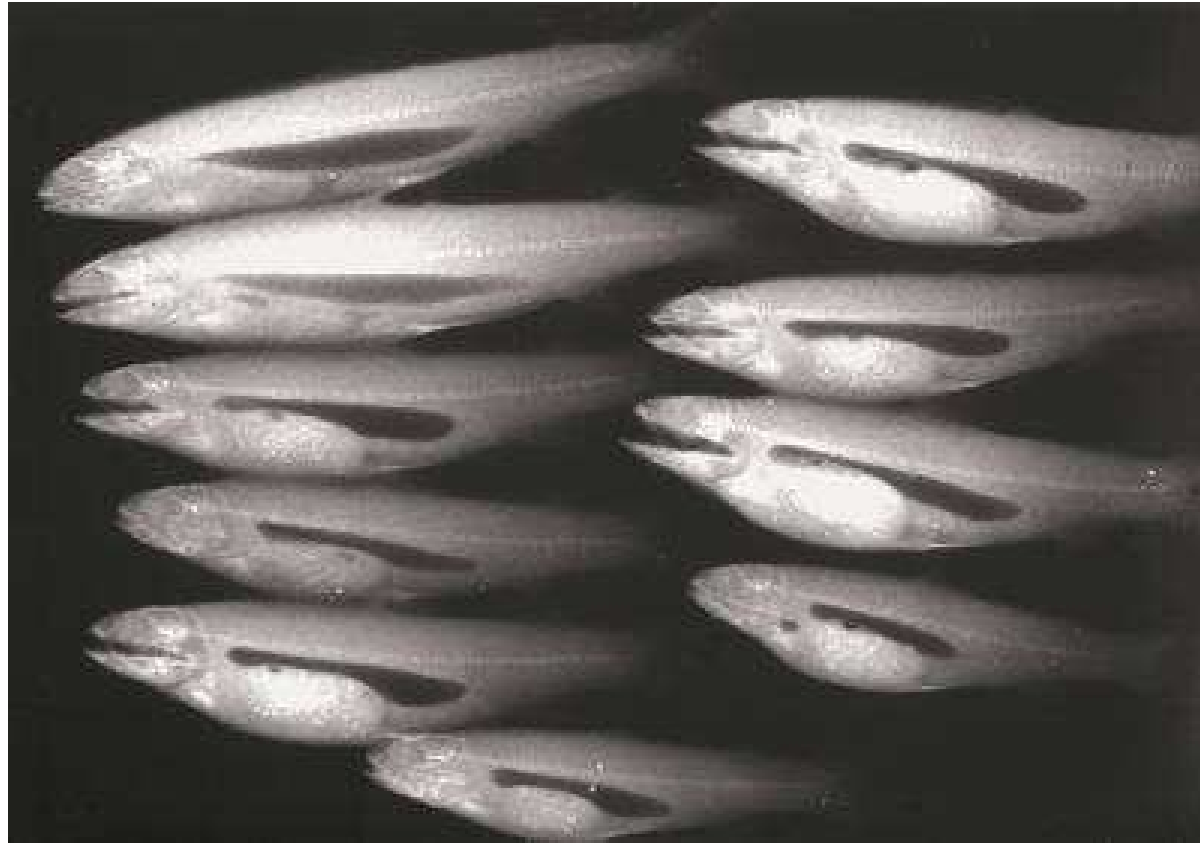
$$c = \sqrt{\frac{g}{k} + \frac{\sigma k}{\rho}}$$

όπου

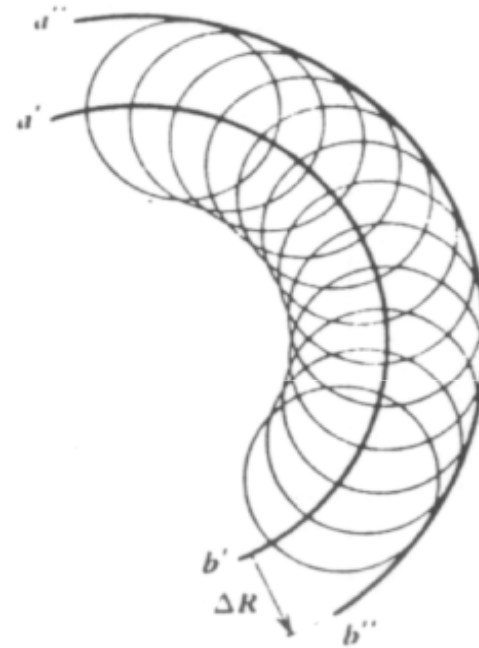
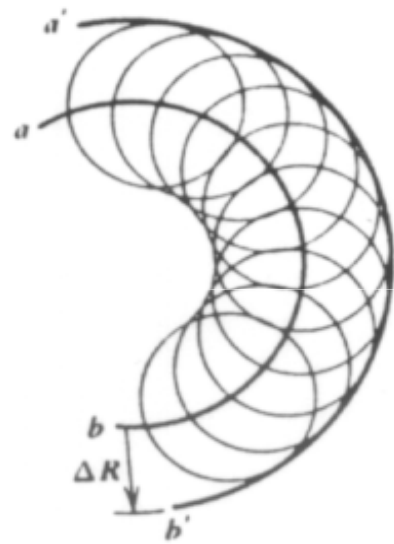
σ είναι η επιφανειακή τάση (τυπική τιμή $7.4 \times 10^{-2} \text{ N/m}$) και
 ρ είναι η πυκνότητα του νερού (kg/m^3).

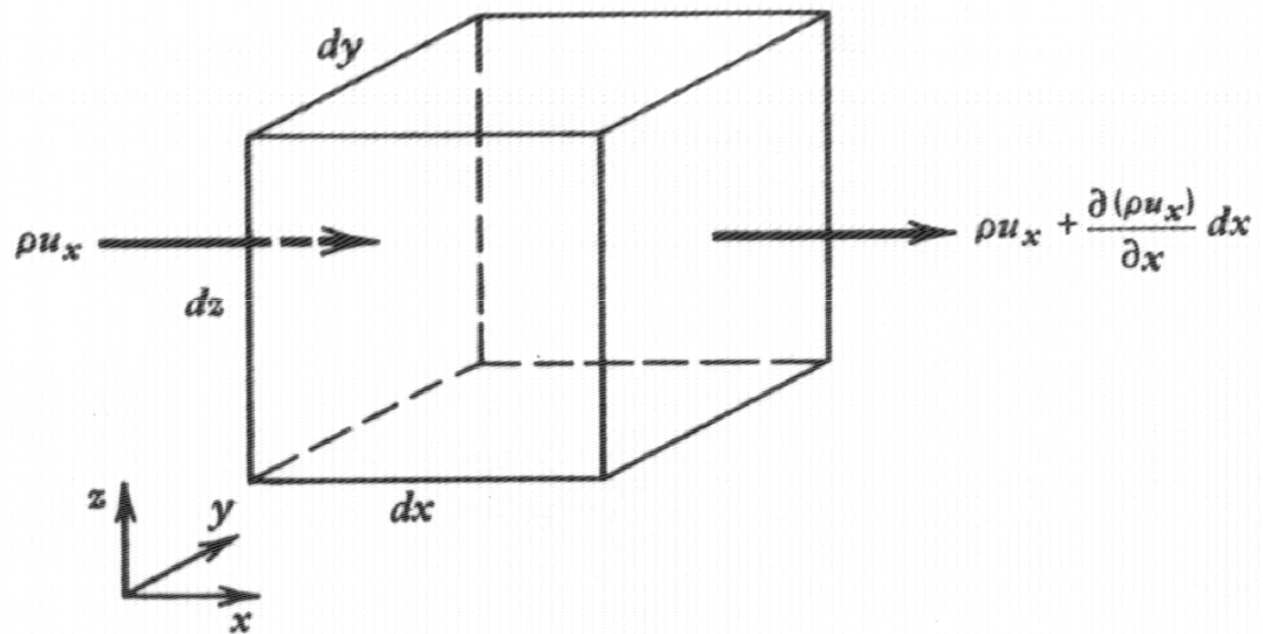










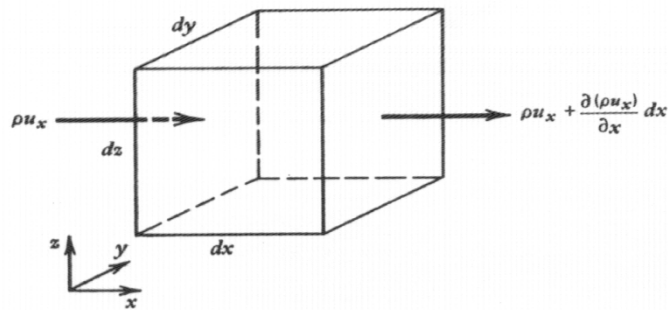


$$\{\rho u_x - [\rho u_x + \frac{\partial(\rho u_x)}{\partial x} dx]\} dydz = -\frac{\partial(\rho u_x)}{\partial x} dV$$

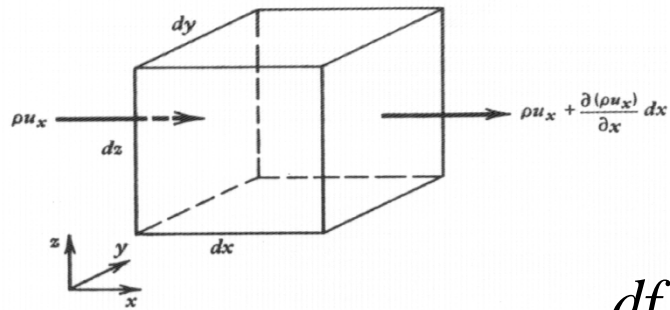
$$-\left[\frac{\partial(\rho u_x)}{\partial x} + \frac{\partial(\rho u_y)}{\partial y} + \frac{\partial(\rho u_z)}{\partial z}\right] dV = -[\nabla \cdot (\rho \vec{u})] dV$$

$$\frac{\partial \rho}{\partial t} dV.$$

$$-[\nabla \cdot (\rho \vec{u})] = \frac{\partial \rho}{\partial t}$$



Εξίσωση συνέχειας



$$d\vec{f} = \vec{a}dm$$

$$df_x = [p - (p + \frac{\partial p}{\partial x} dx)]dydz = -\frac{\partial p}{\partial x} dV$$

$$d\vec{f} = -\nabla p dV$$

$$\vec{a}(x, y, z, t) = \lim_{dt \rightarrow 0} \frac{\vec{u}(x + u_x dt, y + u_y dt, z + u_z dt, t + dt) - \vec{u}(x, y, z, t)}{dt}$$

$$\vec{u} = (x + u_x dt, y + u_y dt, z + u_z dt, t + dt) =$$

$$\vec{u}(x, y, z, t) + \frac{\partial \vec{u}}{\partial t} dt + \frac{\partial \vec{u}}{\partial x} u_x dt + \frac{\partial \vec{u}}{\partial y} u_y dt + \frac{\partial \vec{u}}{\partial z} u_z dt$$

$$\vec{a} dm = -\nabla p dV$$

$$\vec{a} = \frac{\partial \vec{u}}{\partial t} + \frac{\partial \vec{u}}{\partial x} u_x + \frac{\partial \vec{u}}{\partial y} u_y + \frac{\partial \vec{u}}{\partial z} u_z$$

$$\vec{a} = \frac{\partial \vec{u}}{\partial t} + (\vec{u} \cdot \nabla) \vec{u}$$

$$-\nabla p = \rho \left\{ \frac{\partial \vec{u}}{\partial t} + (\vec{u} \cdot \nabla) \vec{u} \right\}$$

Εξίσωση Euler

$$p = g(\rho)$$

Καταστατική Εξίσωση

$$\rho = \rho_0(\vec{x}, t) + \varepsilon \rho_1(\vec{x}, t)$$

$$p = p_0(\vec{x}, t) + \varepsilon p_1(\vec{x}, t)$$

$$\vec{u} = \vec{u}_0(\vec{x}, t) + \varepsilon \vec{u}_1(\vec{x}, t)$$

Εξισ. Συνέχειας

$$\frac{\partial(\rho_0 + \varepsilon \rho_1)}{\partial t} + \nabla \cdot \{(\rho_0 + \varepsilon \rho_1)(\vec{u}_0 + \varepsilon \vec{u}_1)\} = 0$$

$$\frac{\partial \rho_0}{\partial t} + \nabla \cdot \{\rho_0 \vec{u}_0\} = 0$$

$$\frac{\partial \rho_1}{\partial t} + \nabla \cdot \{\rho_0 \vec{u}_1\} = 0$$

Εξισ. Συνέχειας $\frac{\partial \rho_1}{\partial t} + \nabla \cdot \{\rho_0 \vec{u}_1\} = 0$

Εξίσωση Euler $-\nabla p_1 = \rho_0 \frac{\partial \vec{u}_1}{\partial t}$

Καταστατική $p_1 = \frac{\partial p_0}{\partial \rho_0} \rho_1$

$$-\nabla^2 p_1 = \nabla \cdot \left(\rho_0 \frac{\partial \vec{u}_1}{\partial t} \right)$$



$$-\nabla^2 p_1 = -\frac{\partial^2 \rho_1}{\partial t^2}$$

$$\frac{\partial^2 \rho_1}{\partial t^2} + \nabla \cdot \left(\rho_0 \frac{\partial \vec{u}_1}{\partial t} \right) = 0$$

$$\rho_1 = p_1 \frac{1}{\frac{\partial p_0}{\partial \rho_0}}$$

$$\frac{\partial p_0}{\partial \rho_0} \equiv c^2$$

Θερμοδυναμικός Ορισμός
Ταχύτητας

$$\nabla^2 p_1 = \frac{1}{c^2} \frac{\partial^2 p_1}{\partial t^2}$$

Κυματική Εξίσωση

$$p_1(\vec{x}, t) = \bar{p}(\vec{x})T(t)$$

$$\bar{p}(\vec{x}) \equiv p(\vec{x})$$

$$\nabla^2 p_1 = \frac{1}{c^2} \frac{\partial^2 p_1}{\partial t^2}$$

$$T \nabla^2 p = \frac{1}{c^2} p \frac{d^2 T}{dt^2}$$

$$\frac{c^2}{p} \nabla^2 p = \frac{1}{T} \frac{d^2 T}{dt^2}$$

$$\frac{c^2}{p} \nabla^2 p = \frac{1}{T} \frac{d^2 T}{dt^2} = -\omega^2$$

$$\nabla^2 p + \frac{\omega^2}{c^2} p = 0$$

$$\frac{d^2 T}{dt^2} + \omega^2 T = 0$$

$$T = Ae^{i\omega t} + Be^{-i\omega t}$$

$$T = e^{-i\omega t}$$

$$p_1(\vec{x}, t) = \bar{p}(\vec{x})T(t)$$

$$p_1(\vec{x}, t) = p(\vec{x})e^{-i\omega t}$$

$$\nabla^2 p + \frac{\omega^2}{c^2} p = 0$$

$$\nabla^2 \equiv \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$$

$$\left(\frac{\omega}{c}\right)^2 = k^2 = k_x^2 + k_y^2 + k_z^2$$

$$p(x, y, z) = p_x(x)p_y(y)p_z(z)$$

$$\frac{\partial^2 p_x}{\partial x^2} \cdot \frac{1}{p_x} + \frac{\partial^2 p_y}{\partial y^2} \cdot \frac{1}{p_y} + \frac{\partial^2 p_z}{\partial z^2} \cdot \frac{1}{p_z} + k_x^2 + k_y^2 + k_z^2 = 0$$

$$\frac{d^2 p_x}{dx^2} + k_x^2 p_x = 0$$

$$p_x(x) = A_1 e^{ik_x x} + A_2 e^{-ik_x x}$$

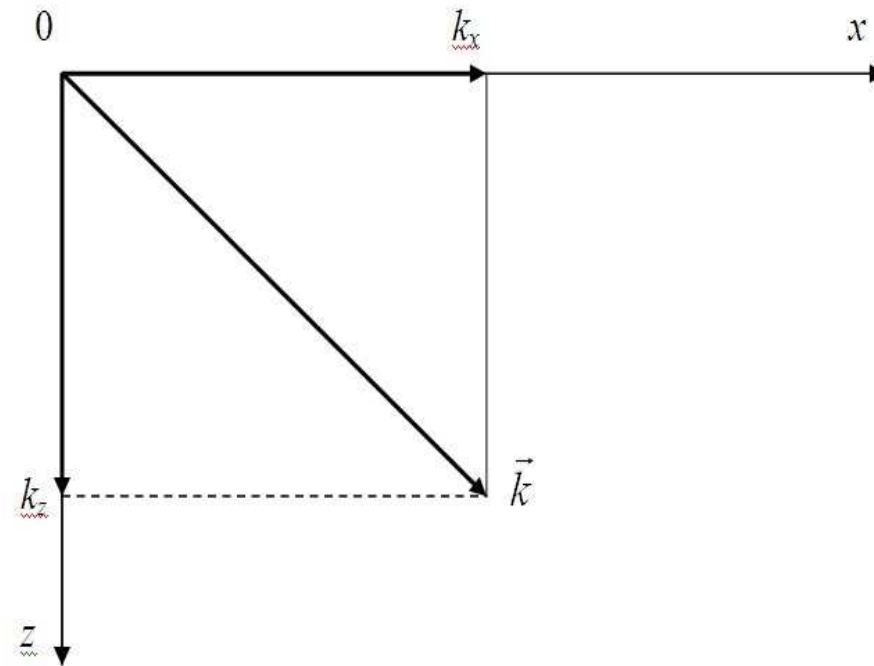
$$\frac{d^2 p_y}{dy^2} + k_y^2 p_y = 0$$

$$p_y(x) = B_1 e^{ik_y y} + B_2 e^{-ik_y y}$$

$$\frac{d^2 p_z}{dz^2} + k_z^2 p_z = 0$$

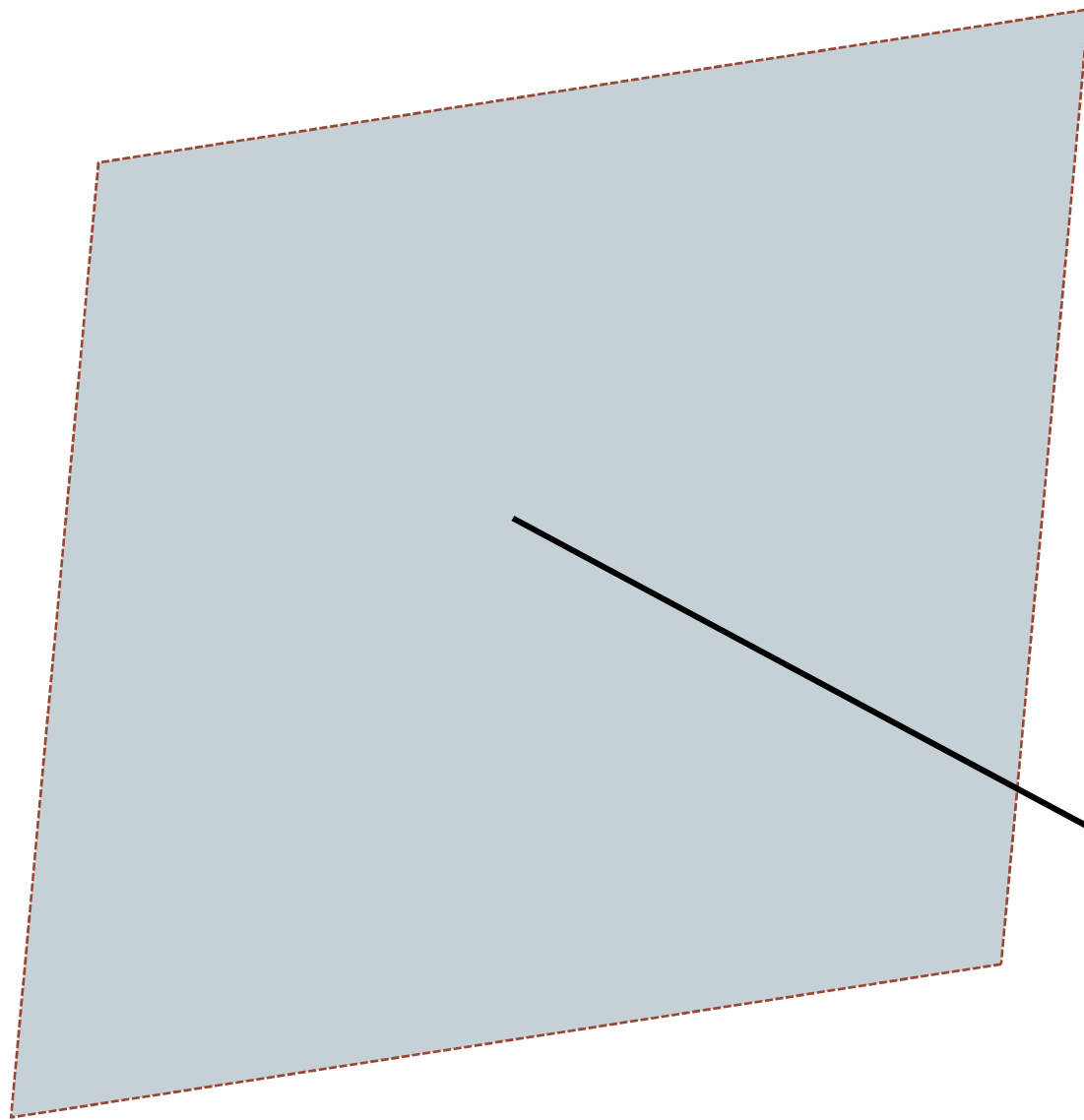
$$p_z(x) = C_1 e^{ik_z z} + C_2 e^{-ik_z z}$$

$$p_1(x,t) = p_x(x)e^{-i\omega t} = (A_1e^{ik_x x} + A_2e^{-ik_x x})e^{-i\omega t} = A_1e^{i(k_x x - \omega t)} + A_2e^{i(-k_x x - \omega t)}$$



$$p_1(x, y, z, t) = A_1 B_1 C_1 e^{i(k_x x + k_y y + k_z z - \omega t)}$$

$$p_1(x, y, z, t) = D e^{i(\vec{k} \cdot \vec{x} - \omega t)}$$



Μέτωπο κύματος

\vec{k}